# Empirics of the Oslo Stock Exchange. Basic, descriptive, results 1980-2016. 

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We give some basic empirical characteristics of the Oslo Stock Exchange in the period after 1980. We give statistics for number of firms, the occurences of IPO's, dividend payments, trading volume, and concentration. Returns for various market indices and portfolios are calculated and described. We also show the well known calendar anomalies, the link between number of stocks in a portfolio and its variance and industry characteristics of the OSE.

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## Chapter 1

## Introduction

This document is a source book for people doing empirical asset pricing using data from the Oslo Stock Exchange (OSE). The prime purpose of the paper is pedagogical, it is to be a useful resource for teaching finance in the Norwegian context. The same purpose is reflected in the lack of discussion of the results, the focus is on the numbers themselves, and students are meant to fill in the details. Having said that, the paper may still be useful for researchers since it summarizes in one place various properties of stock returns on the Norwegian stock exchange.

## New versions

This paper will be updated with new data and additional analysis. The latest version will always be found at my homepage. I am open for suggestions to additional descriptive statistics you'd like to see, but I make no promises.

## Data and data sources

The source data is is daily observations of prices and volume of all stocks listed on the OSE, as well as dividends and adjustement factors necessary for calculating returns. In addition to price data accounting data for all stocks listed at the OSE is used. The data comes from two sources. All accounting and equity data are from OBI (Oslo BørsInformasjon), the data provider of the Oslo Stock Exchange. Interest rate date is from Norges Bank. The data starts in 1980. The stock price data ends in 2016.

## Can you get the indices?

The data from the OSE used in constructing the various indices is governed by an agreement with the exchange that do not allow distribution of data. The raw data on indices and portfolio returns produced in this research is therefore only available to students and researchers at the Norwegian School of Management BI.

However, after agreement from the OSE, a number of constructed indices are made available from my homepage, such as Fama-French factors, portfolio returns for size-sorted indices, and so on.

## The various chapters

Chapter 2 characterizes the evolution of the OSE in the period 1980 to 2016 , by showing time series plots of market values, number of stocks listed, and trading activity. Chapter 3 looks at IPO's, and details the annual number of IPO's at the OSE. Chapter 4 has some numbers on dividends at the OSE. Chapter 5 has some numbers on repurchases at the OSE. Chapter 6 discusses filtering of the data for returns calculations, in particular for asset pricing purposes Chapter 7 shows return statistics for the whole market. Chapter 8
breaks the stocks listed into sectors, shows distribution of sectors, and sector returns. Chapter 9 looks at the importance of a few large stocks. Chapter 10 replicates the classical analysis of e.g. Wagner and Lau (1971) which looks at the link between the number of assets in a portfolio and the variance of the portfolio, illustrated with simulations on Norwegian data. Chapter 11 looks at the volatility of stocks at the OSE. Chapter 13 shows some calendar effects. Chapter 14 details the interest rate data.

### 1.1 Additional papers

In addition to this paper that gives basic characteristics of the exchange, there are three additional papers that looks more detailed at various aspects of the exchange.

A paper with asset pricing results at the OSE looks at crossectional portfolios at the OSE, and construct the factor portfolios of Fama and French (1992) and Carhart (1997) in the Norwegian context.

There is a paper that details liquidity at the OSE, providing time series of various liquidity measures.
Finally, there is a paper giving data on ownership at the OSE.

## Chapter 2

## Characterizing the OSE

In this chapter we look at some aggregate descriptive measures of the Oslo Stock Exhhange

### 2.1 The evolution of market values

Let us start by looking at the aggregate value of all stock on the exchange. Figure 2.1 plots the time series evolution of the total market value of all stocks on the Oslo Stock Exchange.

Figure 2.1 Monthly market values


The plot shows monthly observations of aggregated market values the OSE, in billion NOK. The values are in nominal (current) NOK.

To judge the importance of the stock market in the Norwegian economomy figure 2.2 shows the total market value of all companies at the OSE as a fraction of the annual GDP (Gross Domestic Product) for Norway.

Figure 2.2 Market value OSE relative to annual GDP for Norway


The plot shows annual observations of market values at the OSE, using all stocks on the Exchange, as a percentage fraction of GDP for that year. The data on GDP are from Statistics Norway.

### 2.2 The number of stocks listed

Figure 2.3 Number of active shares at the OSE each month


### 2.3 The evolution of trading activity

A simple measure of the activity at the OSE is the total trading volume in NOK.
Figure 2.4 Quarterly trading volume


The plot shows quarterly trading volume at the OSE, in bill NOK, using all stocks on the Exchange.

Figure 2.5 Quarterly trading volume split size portfolios


Trading volume at the OSE, in mill NOK. Stocks are sorted into four size based portfolios, and then we calculate the aggregate volume for the period.

## Chapter 3

## New listings

In this chapter we give some details on new listings at the OSE (Initial Public Offers - IPOs).

### 3.1 Numbers of new stocks starting to trade at OSE

Figure reffig:newlistings and table 3.1 shows how many firms are introduced at the OSE each year.
Figure 3.1 New listings per year


Each year we count the number of new equities in the OSE stock price data. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

Table 3.1 New listings per year

| Year | Number of new listings |
| :---: | :---: |
| 1980 | 3 |
| 1981 | 3 |
| 1982 | 16 |
| 1983 | 11 |
| 1984 | 20 |
| 1985 | 21 |
| 1986 | 9 |
| 1987 | 9 |
| 1988 | 6 |
| 1989 | 14 |
| 1990 | 11 |
| 1991 | 8 |
| 1992 | 20 |
| 1993 | 19 |
| 1994 | 22 |
| 1995 | 26 |
| 1996 | 24 |
| 1997 | 59 |
| 1998 | 30 |
| 1999 | 11 |
| 2000 | 30 |
| 2001 | 20 |
| 2002 | 7 |
| 2003 | 4 |
| 2004 | 23 |
| 2005 | 48 |
| 2006 | 33 |
| 2007 | 56 |
| 2008 | 17 |
| 2009 | 4 |
| 2010 | 20 |
| 2011 | 13 |
| 2012 | 5 |
| 2013 | 12 |
| 2014 | 19 |
| 2015 | 9 |
| 2016 | 6 |

Each year we count the number of new equities in the OSE stock price data. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

### 3.2 Aggregate values

Figure 3.2 IPO's aggregate values
Panel A: Total value of all new companies at yearend.


Panel B: Comparing total firm values and amounts raised at IPO date.


In the figure in panel $A$ we sum the firm values at yearend for all stocks newly listed on OSE during the year. In the figure in panel $B$ we show the same aggregate values, calculated at the IPO date, together with the aggregate amounts raised during the IPO (lower line). Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

## Chapter 4

## Dividends

In this chapter we describe various aspects of dividend payments at OSE. First we look at the actual dividend amounts per security. Table 4.1 stratifies dividends amounts into four groups: no dividend payment, dividend up to NOK 5, dividend between NOK 5 and NOK 10, and dividend above NOK 10. The most striking feature of the table is the number of stocks which is not paying dividend at all, particularly in the early period. To further illustrate this particular point figure 4.1 shows the fraction of companies on the OSE which is not paying dividends. The figure clearly shows a regime change in dividend payments, where in 1985 close to $75 \%$ of the companies on the OSE did not pay dividends, which had fallen to less than $30 \%$ in 1995. This particular change is most likely a result of a tax change. In 1992 a new tax code was introduced. Under the new code dividends are much less tax disadvantaged. The huge increase in firms starting to pay dividends is most likely a result of this tax code change.

Figure 4.1 What fraction of securities do not pay dividends?


The plot shows what fraction of companies on the OSE does not pay dividend. For each year we count the number of firms listed on the exchange during the year, and the number of those paying dividends. We report what fraction the dividend payers are of the total. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

Table 4.1 How much are companies paying in dividends?

| year | $d=0$ | $d \in(0,5]$ | $d \in(5,10]$ | $d>10$ |
| :--- | ---: | ---: | ---: | ---: |
| 1980 | 66 | 2 | 7 | 21 |
| 1981 | 68 | 3 | 2 | 26 |
| 1982 | 81 | 3 | 0 | 32 |
| 1983 | 96 | 5 | 4 | 24 |
| 1984 | 113 | 16 | 2 | 18 |
| 1985 | 133 | 20 | 5 | 12 |
| 1986 | 146 | 23 | 8 | 7 |
| 1987 | 147 | 28 | 1 | 7 |
| 1988 | 130 | 25 | 3 | 7 |
| 1989 | 140 | 33 | 6 | 2 |
| 1990 | 117 | 59 | 10 | 5 |
| 1991 | 113 | 53 | 3 | 3 |
| 1992 | 109 | 57 | 4 | 2 |
| 1993 | 117 | 59 | 3 | 6 |
| 1994 | 95 | 76 | 19 | 5 |
| 1995 | 80 | 87 | 19 | 8 |
| 1996 | 85 | 88 | 17 | 16 |
| 1997 | 128 | 77 | 24 | 21 |
| 1998 | 135 | 89 | 19 | 26 |
| 1999 | 137 | 81 | 28 | 17 |
| 2000 | 150 | 66 | 13 | 30 |
| 2001 | 148 | 55 | 18 | 26 |
| 2002 | 135 | 51 | 20 | 20 |
| 2003 | 124 | 50 | 24 | 20 |
| 2004 | 110 | 54 | 20 | 23 |
| 2005 | 132 | 59 | 21 | 26 |
| 2006 | 152 | 61 | 21 | 24 |
| 2007 | 184 | 62 | 19 | 27 |
| 2008 | 171 | 69 | 23 | 23 |
| 2009 | 189 | 63 | 10 | 5 |
| 2010 | 163 | 70 | 19 | 7 |
| 2011 | 144 | 78 | 24 | 7 |
| 2012 | 144 | 77 | 16 | 6 |
| 2013 | 132 | 79 | 18 | 11 |
| 2014 | 120 | 81 | 22 | 13 |
| 2015 | 119 | 84 | 15 | 11 |
| 2016 | 121 | 68 | 23 | 9 |
|  |  |  |  |  |

The table illustrates the amount paid in dividends by companies on the OSE. For each stock we find the annual amount of dividend payment per stock. Each year we then calculate the number of stocks with dividends of zero, dividends between zero and five, dividends between five and ten, and dividends above 10. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

Figure 4.2 What are the aggregate dividend payments at the OSE?


The plot shows the total dividend payments (in billions NOK) for all firms at the OSE. For each year we find all firms listed on the exchange during the year, and add the aggregate dividend payment for each firm. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

## Chapter 5

## Repurchases

In this chapter we describe various aspects of repurchase activity at the OSE. Repurchases were legalized for Norwegian firms in 1999. The interesting period is therefore the time after 1999.

Let us first look at the aggregate repurchase activity in the period. The data from the OSE is a list of dates with number of shares bought by the firm from the stock market. The firm can also sell back the shares to the market, which is termed a reverse repurchase. In table 5.1 we aggegate this for all the OSE firms year by year, and calculate total amounts (first three columns) and number of firms (last five columns).

Table 5.1 Repurchase activity for Norwegian Listed Firms

| Year | Aggregate Amounts (mill) |  |  | Number of firms |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Reverse | Net |  | Reverse |  |  | First |
|  | Repur. | Repur. | Repur. | Repurch | Repur. | Total | Both | Time |
| 1999 | 4472 | -177 | 4296 | 51 | 15 | 51 | 15 | 51 |
| 2000 | 5319 | -1902 | 3416 | 63 | 28 | 67 | 24 | 32 |
| 2001 | 6052 | -2037 | 4014 | 74 | 41 | 83 | 32 | 28 |
| 2002 | 1638 | -1175 | 464 | 62 | 39 | 75 | 26 | 11 |
| 2003 | 2210 | -738 | 1472 | 51 | 46 | 67 | 30 | 5 |
| 2004 | 5496 | -3199 | 2297 | 38 | 49 | 61 | 26 | 6 |
| 2005 | 5813 | -2352 | 3461 | 61 | 57 | 81 | 37 | 20 |
| 2006 | 12000 | -4439 | 7561 | 74 | 63 | 91 | 46 | 19 |
| 2007 | 8586 | -2742 | 5844 | 78 | 62 | 94 | 46 | 18 |
| 2008 | 7210 | -1642 | 5568 | 83 | 66 | 101 | 48 | 18 |
| 2009 | 1636 | -1682 | -46 | 44 | 50 | 69 | 25 | 6 |
| 2010 | 4223 | -2121 | 2102 | 52 | 51 | 69 | 34 | 6 |
| 2011 | 6716 | -2585 | 4130 | 61 | 50 | 72 | 39 | 9 |
| 2012 | 6131 | -1813 | 4318 | 45 | 38 | 60 | 23 | 7 |
| 2013 | 4380 | -2864 | 1516 | 49 | 39 | 59 | 29 | 5 |
| 2014 | 4229 | -2051 | 2177 | 56 | 52 | 71 | 37 | 16 |
| 2015 | 4470 | -2826 | 1644 | 53 | 48 | 69 | 32 | 12 |
| 2016 | 3333 | -1585 | 1748 | 49 | 47 | 67 | 29 | 4 |

The table describes repurchase activity at the OSE. The first three columns shows total amounts bought back, the last five columns number of firms involved in repurchase activities.

## Chapter 6

## Filtering of data

The basic data for the empirical investigations in this paper are daily observations of all equities traded at the Oslo Stock exchange. The data contains end of day bid and offer prices, as well as the last trade price of the day, if there was any trading. The data also include the total trading volume at a given date.

Not all stocks traded at the Oslo Stock Exchange should necessarily be used in calculating representative returns for the exchange, for example for empirical asset pricing investigations. In particular stocks which are seldom traded are problematic. In the following, in most calculations we therefore require the stocks to have a minimum number (20) of trading days before they enter the sample. Low valued stocks ("penny stocks") are also problematic since they will have very exaggerated returns. We therefore limit a stocks to have a price above NOK 10 before considering it in the sample. A similar requirement considers total value outstanding, which has a lower limit of NOK 1 million. ${ }^{1}$ Table 6.1 provides some descriptive statistics for this filtering of the sample.

[^0]Table 6.1 Describing securities sample

| year | number of securites listed | average number of trading days | Number of securities with - more than 20 trading days - and price above 10 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1980 | 96 | 48 | 33 | 33 | 33 |
| 1981 | 99 | 60 | 48 | 47 | 47 |
| 1982 | 116 | 60 | 60 | 58 | 58 |
| 1983 | 129 | 106 | 93 | 90 | 90 |
| 1984 | 149 | 127 | 122 | 121 | 121 |
| 1985 | 170 | 145 | 152 | 149 | 149 |
| 1986 | 184 | 135 | 157 | 146 | 146 |
| 1987 | 183 | 133 | 149 | 133 | 133 |
| 1988 | 165 | 118 | 128 | 113 | 113 |
| 1989 | 181 | 131 | 151 | 138 | 138 |
| 1990 | 191 | 127 | 163 | 149 | 149 |
| 1991 | 172 | 132 | 151 | 123 | 123 |
| 1992 | 172 | 111 | 131 | 101 | 101 |
| 1993 | 185 | 139 | 147 | 114 | 114 |
| 1994 | 195 | 139 | 164 | 143 | 143 |
| 1995 | 194 | 149 | 166 | 148 | 148 |
| 1996 | 206 | 161 | 189 | 170 | 169 |
| 1997 | 250 | 158 | 229 | 200 | 199 |
| 1998 | 269 | 146 | 248 | 190 | 190 |
| 1999 | 263 | 152 | 241 | 185 | 185 |
| 2000 | 259 | 157 | 239 | 183 | 183 |
| 2001 | 247 | 150 | 224 | 143 | 143 |
| 2002 | 226 | 147 | 210 | 119 | 119 |
| 2003 | 218 | 150 | 196 | 109 | 109 |
| 2004 | 207 | 180 | 200 | 132 | 132 |
| 2005 | 238 | 182 | 226 | 164 | 164 |
| 2006 | 258 | 181 | 249 | 193 | 193 |
| 2007 | 292 | 179 | 280 | 223 | 223 |
| 2008 | 286 | 178 | 275 | 144 | 144 |
| 2009 | 267 | 173 | 253 | 113 | 113 |
| 2010 | 259 | 188 | 251 | 138 | 138 |
| 2011 | 253 | 191 | 245 | 125 | 125 |
| 2012 | 243 | 187 | 239 | 119 | 119 |
| 2013 | 240 | 189 | 234 | 131 | 131 |
| 2014 | 236 | 195 | 231 | 138 | 138 |
| 2015 | 229 | 204 | 226 | 131 | 131 |
| 2016 | 221 | 217 | 220 | 130 | 130 |
| average | 209 | 149 | 187 | 135 | 135 |

The table provides some descriptive statistics for the sample of equities traded on the Oslo Stock Exchange in the period 1980 to 2016. The first column lists the year. The second column lists the number of stocks listed during the year. The third column the average number of trading days for all listed stocks. The fourth column lists the number of stocks which traded for more than 20 days. The fifth column adds the requirement that the stock did not have a price below NOK 10 . The final column additionally requires an equity market value above 1 mill NOK.

## Chapter 7

## Market portfolios

The first issue we consider is the evolution of the whole market at the Oslo Stock Exchange.

### 7.1 Constructing market portfolios

A typical question is what what one would earn if one invested in stocks at the Oslo Stock Exchange. However, there are (at least two) different ways to answer that question. If one picks a random stock, one wants to find the expected return for the typical stock, in which case an equally weighted average is the relevant measure. Alternatively, one can invest in the whole market, in which case a value weighted average is most relevant. Two indices are constructed to make this measurement. Stocks not satisfying the filter criterion discussed in chapter 6 are removed. Using the remaining stocks equally weighted and value weighted indices are constructed. The indices are constructed to include dividends and other distributions from the stocks. ${ }^{1}$

In addition to these indices two market indices constructed by the Oslo Stock Exchange are used. The OBX is a value weighted index consisting of the thirty most liquid stocks at the stock exchange. This index was constructed to be the basis for derivatives contracts, and initiated at the beginning of 1987. In addition we consider a value weighted index of all stock on the exchange, termed TOT. The Oslo Stock Exchange has changed indices during the period, in the period up to 1999 the total index was called the TOTX. In 1999 this index was replaced by the "All Share Index." TOT is constructed by splicing these two indices. Note that neither of these indices include dividends.

Table 7.1 shows monthly average returns for the various indices for the whole period 1980 till 2016 and for various subperiods.

An alternative view of the difference between equally weighted and value weighted indices is shown in figure 7.1, which illustrates the growth of the two indices in the period from 1980, in nominal terms

Let us also look at this looks in real terms, after correcting for inflation. In figure 7.2 we compare nominal and real numbers.

[^1]Table 7.1 Describing market indices at the Oslo Stock Exchange from 1980
Monthly returns

| Period | index | Returns |  |  |  |  | Dividend Yield mean med |  | Capital Gains |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | mean | (std) | min | med | max |  |  | mean | med |
| 1980-2016 | EW | 1.67 | (5.43) | -18.33 | 1.88 | 19.06 | 0.22 | 0.07 | 1.47 | 1.55 |
|  | VW | 1.86 | (6.13) | -23.78 | 2.43 | 19.72 | 0.22 | 0.03 | 1.66 | 2.16 |
|  | OBX | 0.94 | (6.67) | -29.13 | 1.50 | 18.49 |  |  |  |  |
|  | TOT | 1.22 | (6.23) | -27.42 | 1.81 | 17.45 |  |  |  |  |
| 1980-1985 | EW | 3.03 | (6.23) | -13.87 | 2.19 | 19.06 | 0.13 | 0.00 | 2.98 | 2.00 |
|  | VW | 2.32 | (7.00) | -18.62 | 2.88 | 19.72 | 0.21 | 0.00 | 2.21 | 2.51 |
|  | TOT | 3.37 | (6.24) | -13.52 | 3.26 | 15.91 |  |  |  |  |
| 1985-1989 | EW | 1.60 | (5.75) | -17.93 | 2.13 | 16.96 | 0.06 | 0.00 | 1.53 | 1.84 |
|  | VW | 2.57 | (6.85) | -23.78 | 3.33 | 19.34 | 0.13 | 0.00 | 2.44 | 3.29 |
|  | OBX | 2.41 | (8.57) | -29.13 | 3.82 | 18.49 |  |  |  |  |
|  | TOT | 1.61 | (6.98) | -27.42 | 2.62 | 17.45 |  |  |  |  |
| 1990-1994 | EW | 1.13 | (6.79) | -16.51 | 0.47 | 15.04 | 0.14 | 0.00 | 0.99 | 0.37 |
|  | VW | 1.38 | (6.66) | -14.54 | 2.54 | 13.47 | 0.13 | 0.00 | 1.24 | 2.37 |
|  | OBX | 0.24 | (7.16) | -16.78 | 1.50 | 13.16 |  |  |  |  |
|  | TOT | 0.60 | (6.79) | -16.77 | 2.00 | 12.69 |  |  |  |  |
| 1995-1999 | EW | 2.07 | (4.95) | -18.33 | 2.39 | 12.29 | 0.25 | 0.05 | 1.81 | 2.21 |
|  | VW | 2.30 | (5.49) | -20.55 | 2.39 | 16.71 | 0.19 | 0.02 | 2.11 | 2.14 |
|  | OBX | 1.13 | (5.78) | -23.61 | 1.49 | 16.65 |  |  |  |  |
|  | TOT | 1.42 | (5.55) | -22.57 | 1.62 | 12.49 |  |  |  |  |
| 2000-2004 | EW | 1.43 | (5.36) | -14.37 | 2.12 | 11.58 | 0.32 | 0.11 | 1.13 | 1.67 |
|  | VW | 1.73 | (5.71) | -12.83 | 1.64 | 14.05 | 0.25 | 0.05 | 1.48 | 1.41 |
|  | OBX | 0.45 | (6.50) | -17.29 | 1.01 | 13.17 |  |  |  |  |
|  | TOT | 0.69 | (5.79) | -14.64 | 1.39 | 11.29 |  |  |  |  |
| 2005-2009 | EW | 1.32 | (5.42) | -16.23 | 2.59 | 12.19 | 0.24 | 0.10 | 1.09 | 2.43 |
|  | VW | 1.79 | (7.07) | -21.54 | 3.90 | 14.39 | 0.23 | 0.05 | 1.56 | 3.37 |
|  | OBX | 1.16 | (7.88) | -25.35 | 2.97 | 17.23 |  |  |  |  |
|  | TOT | 1.18 | (7.48) | -23.93 | 3.33 | 15.05 |  |  |  |  |
| 2010-2016 | EW | 1.24 | (2.99) | -7.09 | 1.36 | 7.99 | 0.33 | 0.15 | 0.90 | 1.05 |
|  | VW | 1.33 | (3.90) | -8.55 | 1.54 | 10.96 | 0.34 | 0.17 | 0.99 | 1.16 |
|  | OBX | 0.87 | (4.54) | -10.04 | 0.88 | 10.97 |  |  |  |  |
|  | TOT | 0.86 | (4.29) | -8.84 | 0.97 | 13.15 |  |  |  |  |

The table describes two indices constructed from Norwegian equity market data, one equally weighted and one value weighted, using data starting in 1980. The numbers are percentage monthly returns. mean: (equally weighted) average. med: median. EW: equally weighted index. $V W$ : value weighted index. TOT: Total index provided by OSE: 1993-1999: TOTX, Afterwards: All Share Index. $O B X$ : Index provided by OSE. Contains the 30 most liquid stocks at the OSE. Note that OBX starts in January 1987. Returns are percentage monthly returns. The returns are not annualized. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

Figure 7.1 The evolution of market indicies


The figures illustrates the growth of two OSE stock indices, one equally weighted and one value weighted, using data starting in 1980. Growth is shown by finding how much one NOK invested in January 1980 would have grown to. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

Figure 7.2 The evolution of market indicies correcting for inflation


The figures illustrates the growth of the equally weighted OSE stock indicex, using data starting in 1980. Growth is shown by finding how much one NOK invested in January 1980 would have grown to in respectively nominal and real terms (i.e. in 1980 values). Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

To see how "different" the indices are table 7.2 show the correlations of their returns.
Table 7.2 Correlations between alternative market indices
Panel A: Monthly returns

|  | ew | vw | tot |
| :--- | :---: | :---: | :---: |
| vw | 0.88 |  |  |
| tot | 0.91 | 0.98 |  |
| obx | 0.88 | 0.97 | 0.98 |

Panel B: Weekly returns

|  | ew | vw | tot |
| :--- | :---: | :---: | :---: |
| vw | 0.82 |  |  |
| tot | 0.81 | 0.97 |  |
| obx | 0.84 | 0.96 | 0.98 |

Panel C: Daily returns

|  | ew | vw | tot |
| :--- | :---: | :---: | :---: |
| vw | 0.84 |  |  |
| tot | 0.84 | 0.98 |  |
| obx | 0.83 | 0.98 | 0.98 |

The tables shows correlations between index returns for various market indices at the Oslo Stock Exchange. EW: equally weighted index. $V W$ : value weighted index. TOT: Total index provided by OSE: 1993-1999: TOTX, Afterwards: All Share Index. OBX: Index provided by OSE. Contains the 30 most liquid stocks at the OSE. Note that OBX starts in January 1987.

### 7.2 The equity premium

The equity premium is the return of a stock or a stock portfolio in excess of a risk free return

$$
e r_{i}=r_{i}-r_{f}
$$

where $r_{i}$ is the return on a stock or a stock index, and $r_{f}$ a risk free rate. Whether the average return on equity is "too high" to be justified is a a long standing issue in finance. ${ }^{2}$ In this section some estimates of the equity premium are calculated.

Let us start by using monthly observations of stock index returns. Let $r_{m t}$ be the market return observed at date $t$. This is an ex post return calculated as $r_{m t}=\frac{x_{t}-x_{t-1}}{x_{t-1}}$, where $x_{t}$ is the index level at time $t$. If this is a monthly return, the relevant risk free interest rate is the one month interest rate observed at date $t-1$, because this is the interest rate that can be guaranteed for the period $t-1$ to $t$. The excess return is thus calculated as

$$
e r_{t}=r_{m t}-r_{f, t-1}
$$

where $r_{f, t-1}$ is the one month interest rate observed at date $t-1$. Table 7.3 shows estimates of this monthly excess market return.

[^2]Table 7.3 Excess returns of market indices at the Oslo Stock Exchange from 1982
Monthly excess returns


The table describes market indices for the Oslo Stock Exchange using data starting in 1982. (The risk free rate is only available from 1982.) The numbers are percentage monthly excess returns, returns in excess of the risk free rate. $E W$ : equally weighted index. $V W$ : value weighted index. OBX: Index provided by OSE. Contains the 30 most liquid stocks at the OSE. Note that OBX starts in January 1987. TOT: Total index provided by OSE: 1993-1999: TOTX, Afterwards: All Share Index. Returns are percentage monthly returns. The returns are not annualized. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

However, it it not clear that one want to use this high frequency data to estimate the longer term equity premium. One problem is that the monthly risk free rate is rather volatile. ${ }^{3}$

An alternative is to use annual index returns and annual interest rates. Table 7.4 gives estimates of annual excess returns using a one year interest rate.

Table 7.4 Annual excess returns
Annual excess returns

| Index | Period | Average Annual Excess Return |
| :--- | :---: | :---: |
| EW | $(1980-2016)$ | 18.38 |
| VW | $(1980-2016)$ | 21.49 |
| OBX | $(1987-2016)$ | 6.26 |
| TOT | $(1983-2016)$ | 9.82 |

$E W$ : equally weighted index. $V W$ : value weighted index. $O B X$ : Index provided by OSE. Contains the 30 most liquid stocks at the OSE. Note that OBX starts in January 1987. TOT: Total index provided by OSE: 1993-1999: TOTX, Afterwards: All Share Index. Note that the risk free rate series starts in 1982.

[^3]
### 7.3 Sharpe Ratios for market indices

The Sharpe ratio is a relative measure of how much return one gets per unit of risk, where risk is measured by the standard deviation. The Sharpe ratio is defined as

$$
S R_{i}=\frac{E\left[r_{i}\right]-r_{f}}{\sigma\left(r_{i}-r_{f}\right)}
$$

The Sharpe Ratios in table 7.5 are estimated by replacing $E\left[r_{i}-r_{f}\right]$ and $\sigma\left(r_{i}-r_{f}\right)$ by their sample averages.
Table 7.5 Sharpe ratios market indices at the Oslo Stock Exchange from 1980
Monthly returns

|  | EW | VW |
| :---: | :---: | :---: |
| $1980-2016$ | 0.20 | 0.21 |
| $1980-1989$ | 0.21 | 0.18 |
| $1990-1999$ | 0.16 | 0.20 |
| $2000-2016$ | 0.23 | 0.23 |
| $1980-1984$ | 0.33 | 0.16 |
| $1985-1989$ | 0.08 | 0.21 |
| $1990-1994$ | 0.05 | 0.08 |
| $1995-1999$ | 0.33 | 0.34 |
| $2000-2004$ | 0.18 | 0.22 |
| $2005-2009$ | 0.19 | 0.21 |
| $2010-2016$ | 0.37 | 0.30 |

The table shows ex post Sharpe ratios for market indices constructed from Norwegian equity market data. Note that the Sharpe ratios are not annualized. $E W$ : equally weighted index. $V W$ : value weighted index. $O B X$ : Index provided by OSE. Contains the 30 most liquid stocks at the OSE. Note that OBX starts in January 1987. TOT: Total index provided by OSE: 1993-1999: TOTX, Afterwards: All Share Index. Returns are percentage monthly returns. The returns are not annualized. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

### 7.4 Distribution of market returns

The statistical descriptions of the previous chapters does not give a complete picture of the distributional properties of the market returns. One way to show more detail is to plot the actual distributions. Figures 7.3, 7.4 and 7.5 shows histograms of respectively monthly, weekly and daily returns for the EW index.

Figure 7.3 Histogram of monthly stock returns


The figure shows the distribution of monthly stock return for the EW index. EW: equally weighted index. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

Figure 7.4 Histogram of weekly stock returns


The figure shows the distribution of weekly stock return for the EW index. $E W$ : equally weighted index. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

Figure 7.5 Histogram of daily stock returns


The figure shows the distribution of daily stock return for the EW index. $E W$ : equally weighted index. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016. Calculations use the stocks satisfying the "filter" criteria discussed in chapter 6.

### 7.5 Some alternative portfolios

In addition to the broad market indices $E W$ and $V W$ a couple of alternative indices are constructed. If we want to make an investment in the market, but worry about transaction costs, one solution is to invest in a lower number of stocks. To look at how representative such portfolios are we construct indices using the 20 largest stocks at the OSE. Two such portfolios are calculated, 20EW and 20VW. For both indices we choose the 20 largest stocks at the beginning of the year. These stocks are then used to create portfolios for the next year, either equally weighted or value weighted. At each yearend the sample of stocks is changed to be the 20 largest stocks at that time.

Table 7.6 Some special indices at the Oslo Stock Exchange from 1980
Average returns

| Period | index | Returns |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | mean | $($ std $)$ | min | med | max |
| $1980-2016$ | 20EW | 1.00 | $(6.82)$ | -29.82 | 1.54 | 17.81 |
|  | 20VW | 1.55 | $(6.44)$ | -28.07 | 1.90 | 21.78 |
| $1980-1985$ | 20EW | 1.99 | $(6.15)$ | -14.41 | 1.49 | 17.81 |
|  | 20VW | 1.77 | $(7.33)$ | -19.23 | 1.90 | 21.78 |
| $1985-1989$ | 20EW | 1.46 | $(7.34)$ | -28.71 | 2.40 | 17.03 |
|  | 20VW | 2.36 | $(7.58)$ | -28.07 | 2.89 | 17.92 |
| $1990-1994$ | 20EW | 0.43 | $(7.29)$ | -18.83 | 1.50 | 12.59 |
|  | 20VW | 1.18 | $(6.65)$ | -14.67 | 2.45 | 12.69 |
| $1995-1999$ | 20EW | 1.48 | $(5.71)$ | -24.98 | 1.42 | 14.50 |
|  | 20VW | 1.78 | $(5.55)$ | -23.11 | 1.80 | 14.57 |
| $2000-2004$ | 20EW | 0.41 | $(7.69)$ | -24.37 | 1.26 | 16.44 |
|  | 20VW | 1.54 | $(5.93)$ | -16.43 | 1.67 | 14.78 |
| $2005-2009$ | 20EW | 0.97 | $(8.22)$ | -29.82 | 2.81 | 14.31 |
|  | 20VW | 1.54 | $(7.55)$ | -22.90 | 3.89 | 14.75 |
| $2010-2016$ | 20EW | 0.52 | $(5.07)$ | -13.46 | 0.37 | 12.33 |
|  | 20VW | 1.10 | $(4.18)$ | -9.04 | 1.22 | 11.32 |

Correlations with other indices

|  | 20 ew | 20 vw |
| :--- | :---: | :---: |
| 20 vw | 0.92 |  |
| ew | 0.88 | 0.81 |
| vw | 0.93 | 0.98 |
| tot | 0.95 | 0.96 |
| obx | 0.96 | 0.97 |

The table describes indices for the Oslo Stock Exchange using data starting in 1980. The numbers are percentage monthly returns.

## Chapter 8

## Industry sectors (GICS)

### 8.1 The GICS standard

The Global Insustry Classification Standard (GICS) is a grouping of companies into industry sectors. The GICS standard was introduced by Morgan Stanley Capital International (MSCI). It has since been adopted by many stock exchanges throughout the world. The Oslo Stock Exchange groups the companies on the exchange using the industry categories of the standard. The standard groups companies into one of the 10 groups listed in table 8.1.

| Table 8.1 The GICS standard |  |  |
| :--- | :--- | :--- |
|  | English | Norwegian |
| 10 | Energy and consumption | Energi |
| 15 | Material/labor | Materialer |
| 20 | Industrials | Industri |
| 25 | Consumer Discretionary | Forbruksvarer |
| 30 | Consumer Staples | Konsumentvarer |
| 35 | Health Care/liability | Helsevern |
| 40 | Financials | Finans |
| 45 | Information Technology | Informasjonsteknologi (IT) |
| 50 | Telecommunication Services | Telekommunikasjon og tjenester |
| 55 | Utilities | Forsyningsselskaper |

In the fall of 2016 the GICS standard was amended by adding a sector 60, Real Estate. Some of the industries on the OSE was reclassified into this sector. In the following tables we do not include this reclassification. It will be added for the 2017 data.

### 8.2 Grouping firms on the Oslo Stock Exchange

The Oslo Stock Exchange has since 1997 been using the GICS standard to group the firms on the exchange. We use the OSE classification. For firms delisted before 1997 the OSE does not provide a classification. The classification for the missing firms have been backfilled manually for the period 1980-1997. To see how the firms on the OSE distibutes by category table 8.3 shows, for each year, the number of active firms in each of the 10 categories. The companies are clearly concentrated into a few sectors. For the early part of the period, the two sectors with most companies are 20, Industrials, and 40, Financials. This pattern changes in the last 15 years, with 10, Energy (which includes oil related companies), and 45, IT, showing a marked increase. For some sectors, there is a paucity of companies on the OSE. Both categories Health Care (35)
and Utilites (55) are in fact empty till the mid nineties. The OSE is concentrated in only a few of the 10 GICS categories.

Table 8.2 The distribution across industries
Panel A: Number of Companies

|  | Whole |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Industry | Period | $1980-89$ | $1990-99$ | $2000-09$ | $2010-$ |
| 10 Energy | 30.7 | 14.7 | 25.5 | 52.0 | 67.6 |
| 15 Material | 10.8 | 11.4 | 10.5 | 10.5 | 10.1 |
| 20 Industry | 50.3 | 42.9 | 58.9 | 49.0 | 44.1 |
| 25 ConsDisc | 16.7 | 13.0 | 19.2 | 17.8 | 11.0 |
| 30 ConsStapl | 8.6 | 9.1 | 4.4 | 12.4 | 15.1 |
| 35 Health | 5.5 | 1.7 | 3.3 | 11.4 | 16.4 |
| 40 Finan | 37.7 | 33.3 | 36.6 | 43.2 | 42.7 |
| 45 IT | 23.5 | 8.3 | 18.9 | 43.2 | 26.7 |
| 50 Telecom | 1.0 | 0.5 | 0.5 | 1.9 | 2.6 |
| 55 Util | 0.7 | 0.0 | 0.4 | 1.7 | 3.0 |

Panel B: Fraction of value

|  | Whole |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Industry | Period | $1980-89$ | $1990-99$ | $2000-09$ | $2010-$ |
| 10 Energy | 24.0 | 9.9 | 19.2 | 43.0 | 39.9 |
| 15 Material | 6.4 | 10.3 | 6.0 | 2.8 | 0.7 |
| 20 Industry | 29.7 | 40.0 | 35.4 | 13.6 | 12.5 |
| 25 ConsDisc | 5.8 | 4.0 | 7.2 | 6.1 | 8.9 |
| 30 ConsStapl | 7.4 | 6.9 | 8.8 | 6.5 | 8.1 |
| 35 Health | 5.4 | 4.0 | 7.8 | 4.3 | 1.1 |
| 40 Finan | 16.3 | 21.3 | 15.6 | 12.1 | 16.6 |
| 45 IT | 5.4 | 6.5 | 3.8 | 6.0 | 2.9 |
| 50 Telecom | 3.4 | 0.0 | 0.8 | 9.4 | 11.2 |
| 55 Util | 0.5 | 0.0 | 0.4 | 1.1 | 1.0 |

In the table we first calculate numbers for each year, and then report averages across years. The top table counts the number of firms on the exchange. The second the fraction of the value of the exchange (at yearend) in each sector.

### 8.3 Sector indices

The company distribution listed in table 8.3 is the basis for construction of sector indices for the OSE. Using the standard liquidity criteria discussed in chapter 6 . Table 8.5 describes average monthly returns for the 10 indices. In table 8.6 the correlations between the same 10 indices are calculated.

### 8.4 References

The GICS standard is described in the Wikipedia (en.wikipedia.org), as well as at the homepages of Morgan Stanley (www.msci.com) and Standard and Poors (www.standardandpoors.com).

Table 8.3 The number of companies in the different GICS Industry Sectors
Panel A: Subperiod 1980-1989

|  | 1980 | 1981 | 1982 | 1983 | 1984 | 1985 | 1986 | 1987 | 1988 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 9 | 9 | 12 | 12 | 14 | 17 | 18 | 20 | 19 |
| Material/labor | 10 | 11 | 12 | 11 | 12 | 12 | 12 | 12 | 11 |
| Industrials | 29 | 29 | 34 | 39 | 45 | 52 | 55 | 51 | 49 |
| Consumer Discretionary | 6 | 7 | 12 | 13 | 15 | 18 | 18 | 16 | 14 |
| Consumer Staples | 9 | 9 | 9 | 9 | 10 | 11 | 11 | 9 | 7 |
| Health Care/liability | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 |
| Financials | 27 | 28 | 29 | 30 | 36 | 37 | 39 | 39 | 32 |
| Information Technology | 2 | 2 | 3 | 6 | 7 | 13 | 13 | 13 | 12 |
| Telecommunication Services | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 2 | 2 |
| Utilities | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| All | 93 | 96 | 112 | 122 | 141 | 162 | 169 | 164 | 148 |

Panel B: Subperiod 1990-1999

|  | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 21 | 22 | 21 | 20 | 20 | 21 | 25 | 38 | 35 |
| Material/labor | 9 | 9 | 9 | 9 | 10 | 11 | 12 | 13 | 12 |
| Industrials | 50 | 45 | 46 | 54 | 59 | 61 | 58 | 69 | 75 |
| Consumer Discretionary | 10 | 9 | 14 | 17 | 18 | 21 | 22 | 25 | 28 |
| Consumer Staples | 7 | 5 | 3 | 4 | 3 | 2 | 3 | 5 | 6 |
| Health Care/liability | 2 | 2 | 2 | 2 | 3 | 3 | 3 | 5 | 5 |
| Financials | 36 | 30 | 30 | 29 | 32 | 39 | 39 | 39 | 45 |
| Information Technology | 11 | 10 | 10 | 10 | 11 | 14 | 21 | 29 | 34 |
| Telecommunication Services | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| Utilities | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| All | 146 | 132 | 135 | 145 | 156 | 172 | 185 | 225 | 242 |

Panel C: Subperiod 2000-2009

|  | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 33 | 35 | 35 | 36 | 34 | 52 | 61 | 84 | 79 | 71 |
| Material/labor | 13 | 9 | 9 | 8 | 9 | 9 | 10 | 14 | 12 | 12 |
| Industrials | 60 | 58 | 49 | 42 | 41 | 43 | 45 | 50 | 52 | 50 |
| Consumer Discretionary | 25 | 22 | 20 | 21 | 18 | 16 | 18 | 13 | 13 | 12 |
| Consumer Staples | 6 | 8 | 9 | 8 | 9 | 13 | 14 | 18 | 20 | 19 |
| Health Care/liability | 7 | 7 | 7 | 8 | 10 | 11 | 13 | 16 | 18 | 17 |
| Financials | 48 | 45 | 44 | 42 | 38 | 43 | 40 | 46 | 43 | 43 |
| Information Technology | 49 | 44 | 43 | 40 | 41 | 46 | 47 | 43 | 43 | 36 |
| Telecommunication Services | 3 | 2 | 2 | 2 | 1 | 1 | 2 | 2 | 2 | 2 |
| Utilities | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| All | 245 | 231 | 219 | 209 | 203 | 236 | 252 | 288 | 284 | 264 |

Panel D: Subperiod 2010-2016

|  | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 68 | 72 | 67 | 71 | 70 | 64 | 61 |
| Material/labor | 12 | 12 | 11 | 10 | 10 | 9 | 7 |
| Industrials | 47 | 45 | 45 | 42 | 45 | 43 | 42 |
| Consumer Discretionary | 13 | 11 | 11 | 10 | 11 | 11 | 10 |
| Consumer Staples | 19 | 18 | 18 | 18 | 13 | 10 | 10 |
| Health Care/liability | 17 | 18 | 17 | 17 | 15 | 16 | 15 |
| Financials | 44 | 45 | 45 | 41 | 40 | 41 | 43 |
| Information Technology | 32 | 28 | 25 | 27 | 26 | 27 | 22 |
| Telecommunication Services | 2 | 2 | 2 | 3 | 3 | 3 | 3 |
| Utilities | 2 | 2 | 2 | 3 | 4 | 4 | 4 |
| All | 256 | 253 | 243 | 242 | 237 | 228 | 217 |

The tables list, for each year, the number of active firms on the exchange in each GICS sector. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

Table 8.4 The fraction of market values in the different GICS Industry Sectors Panel A: Subperiod 1980-1989

|  | 1980 | 1981 | 1982 | 1983 | 1984 | 1985 | 1986 | 1987 | 1988 | 1989 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 10.80 | 9.50 | 8.46 | 8.77 | 8.93 | 8.14 | 7.00 | 10.01 | 10.42 | 16.58 |
| Material/labor | 8.86 | 8.95 | 8.25 | 10.10 | 10.82 | 11.08 | 11.09 | 11.75 | 10.47 | 12.03 |
| Industrials | 57.95 | 50.83 | 39.25 | 36.68 | 32.60 | 32.87 | 34.30 | 32.93 | 42.69 | 40.36 |
| Consumer Discretionary | 1.01 | 1.53 | 3.19 | 2.38 | 3.55 | 5.73 | 7.68 | 6.31 | 5.31 | 3.40 |
| Consumer Staples | 2.30 | 4.75 | 5.50 | 5.02 | 6.87 | 6.45 | 10.00 | 11.42 | 7.80 | 8.50 |
| Health Care/liability | 1.13 | 1.23 | 2.34 | 3.43 | 3.31 | 4.43 | 3.62 | 5.91 | 9.34 | 5.67 |
| Financials | 18.29 | 23.89 | 27.13 | 21.40 | 21.78 | 20.91 | 23.61 | 24.96 | 14.47 | 16.56 |
| Information Technology | 0.81 | 3.73 | 5.96 | 12.23 | 12.15 | 10.49 | 10.11 | 5.27 | 2.74 | 1.85 |
| Telecommunication Services | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.10 | 0.18 | 0.10 | 0.00 |
| Utilities | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |

Panel B: Subperiod 1990-1999

|  | 1990 | 1991 | 1992 | 1993 | 1994 | 1995 | 1996 | 1997 | 1998 | 1999 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 21.72 | 22.63 | 19.10 | 17.80 | 15.76 | 16.37 | 23.57 | 24.57 | 15.46 | 15.38 |
| Material/labor | 8.14 | 6.49 | 6.04 | 8.02 | 8.13 | 6.66 | 4.57 | 2.95 | 3.69 | 5.17 |
| Industrials | 39.32 | 40.16 | 40.23 | 36.94 | 40.88 | 37.97 | 35.38 | 27.84 | 27.40 | 28.05 |
| Consumer Discretionary | 2.63 | 2.15 | 4.91 | 5.82 | 5.24 | 5.00 | 5.70 | 9.33 | 15.08 | 16.45 |
| Consumer Staples | 10.45 | 11.53 | 15.32 | 11.81 | 6.41 | 6.49 | 6.84 | 6.28 | 6.38 | 6.23 |
| Health Care/liability | 6.58 | 11.19 | 12.29 | 5.69 | 5.36 | 6.15 | 2.59 | 8.38 | 14.20 | 5.60 |
| Financials | 16.40 | 8.54 | 8.52 | 16.54 | 18.16 | 20.32 | 17.36 | 14.70 | 18.40 | 17.16 |
| Information Technology | 1.81 | 1.50 | 1.76 | 1.98 | 1.35 | 3.59 | 4.62 | 4.69 | 5.37 | 11.27 |
| Telecommunication Services | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.70 | 1.33 | 2.04 | 3.74 |
| Utilities | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.28 | 0.75 | 1.04 | 0.76 |

Panel C: Subperiod 2000-2009

|  | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 9.84 | 25.94 | 42.41 | 42.58 | 42.96 | 51.70 | 51.13 | 50.39 | 60.86 | 52.21 |
| Material/labor | 5.25 | 4.72 | 3.94 | 3.59 | 3.23 | 2.70 | 1.72 | 1.28 | 0.59 | 0.57 |
| Industrials | 27.17 | 26.36 | 9.49 | 6.85 | 10.32 | 11.26 | 10.49 | 10.84 | 11.99 | 11.40 |
| Consumer Discretionary | 10.04 | 5.78 | 6.47 | 8.31 | 9.07 | 6.17 | 4.48 | 3.46 | 3.24 | 3.81 |
| Consumer Staples | 7.92 | 6.73 | 7.04 | 5.09 | 5.62 | 5.77 | 6.36 | 7.01 | 6.52 | 7.00 |
| Health Care/liability | 7.49 | 7.94 | 8.01 | 8.56 | 7.59 | 0.38 | 0.38 | 0.70 | 1.17 | 0.97 |
| Financials | 17.20 | 14.51 | 14.91 | 12.81 | 13.90 | 11.21 | 10.32 | 9.20 | 6.48 | 10.67 |
| Information Technology | 10.62 | 7.17 | 3.69 | 4.30 | 4.40 | 3.87 | 6.20 | 8.58 | 6.32 | 4.93 |
| Telecommunication Services | 13.26 | 9.20 | 8.54 | 9.94 | 9.65 | 7.63 | 9.91 | 9.63 | 7.66 | 8.85 |
| Utilities | 0.60 | 0.54 | 0.91 | 1.03 | 0.92 | 1.10 | 1.33 | 1.54 | 1.72 | 1.14 |

Panel C: Subperiod 2000-2016

|  | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Energy and consumption | 44.04 | 51.42 | 46.62 | 42.28 | 32.85 | 26.90 | 35.53 |
| Material/labor | 1.43 | 1.14 | 0.56 | 0.29 | 0.44 | 0.45 | 0.72 |
| Industrials | 12.72 | 12.16 | 13.14 | 11.22 | 11.81 | 13.43 | 13.27 |
| Consumer Discretionary | 6.52 | 4.92 | 5.95 | 6.40 | 11.96 | 16.06 | 10.48 |
| Consumer Staples | 7.49 | 5.56 | 6.66 | 6.58 | 8.55 | 9.54 | 12.04 |
| Health Care/liability | 0.95 | 1.16 | 1.05 | 1.38 | 1.16 | 0.47 | 1.67 |
| Financials | 14.15 | 12.92 | 14.41 | 17.35 | 18.45 | 18.44 | 20.80 |
| Information Technology | 4.27 | 2.15 | 1.95 | 2.92 | 3.31 | 3.14 | 2.34 |
| Telecommunication Services | 9.56 | 11.20 | 11.75 | 12.26 | 12.62 | 11.73 | 9.53 |
| Utilities | 1.05 | 1.07 | 0.84 | 0.71 | 0.91 | 0.99 | 1.35 |

The tables list, for each year, the percentage fraction of the value of the OSE is in each GICS sector. Measurement done at yearend. Data for the period 1980-2016.

Table 8.5 Industry returns
Panel A: Equally weighted industry indices
$\left.\begin{array}{lcccccc} & \begin{array}{c}\text { First } \\ \text { year }\end{array} & \begin{array}{c}\text { Last } \\ \text { year }\end{array} & \begin{array}{c}\text { Average } \\ \text { return }\end{array} & \begin{array}{c}\text { Standard } \\ \text { deviation }\end{array} & \begin{array}{c}\text { average }\end{array} & n\end{array}\right] T$

Panel B: Value weighted industry indices

|  | First <br> year | Last <br> year | Average <br> return | Standard <br> deviation | average <br> $n$ | $T$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 Energy(vw) | 1980 | 2016 | 1.72 | 7.89 | 20.5 | 444 |
| 15 Material(vw) | 1980 | 2016 | 1.73 | 11.93 | 6.1 | 444 |
| 20 Industry(vw) | 1980 | 2016 | 1.71 | 7.26 | 31.6 | 444 |
| 25 ConsDisc(vw) | 1980 | 2016 | 2.33 | 10.24 | 10.3 | 444 |
| 30 ConsStapl(vw) | 1980 | 2016 | 2.16 | 7.28 | 7.0 | 444 |
| 35 Health(vw) | 1980 | 2016 | 1.89 | 8.55 | 4.6 | 444 |
| 40 Finan(vw) | 1980 | 2016 | 1.54 | 6.83 | 28.3 | 444 |
| 45 IT(vw) | 1980 | 2016 | 3.07 | 13.04 | 11.3 | 444 |
| 50 Telecom(vw) | 1987 | 2016 | 1.26 | 10.21 | 1.6 | 260 |
| 55 Util(vw) | 1996 | 2016 | 1.01 | 6.68 | 2.7 | 252 |

The table describes portfolio returns of 10 industry portfolios gruoped by GICS. We report the first and last years of each index, the average monthly return (in percent), the average number of equities in the portfolio (avg $n$ ), and the number of months of returns used in the calculation $(T)$. The index described in Panel A is an equally weighted index using all stocks in a given industry.

Table 8.6 Correlations across industry sectors
Panel A: Equally weighted industry indices

|  | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 Material(ew) | 0.37 |  |  |  |  |  |  |  |  |
| 20 Industry(ew) | 0.73 | 0.48 |  |  |  |  |  |  |  |
| 25 ConsDisc(ew) | 0.47 | 0.50 | 0.60 |  |  |  |  |  |  |
| 30 ConsStapl(ew) | 0.53 | 0.41 | 0.59 | 0.49 |  |  |  |  |  |
| 35 Health(ew) | 0.40 | 0.28 | 0.47 | 0.38 | 0.36 |  |  |  |  |
| 40 Finan(ew) | 0.61 | 0.45 | 0.68 | 0.57 | 0.58 | 0.36 |  |  |  |
| 45 IT(ew) | 0.54 | 0.26 | 0.49 | 0.45 | 0.43 | 0.46 | 0.45 |  |  |
| 50 Telecom(ew) | 0.39 | 0.18 | 0.36 | 0.37 | 0.27 | 0.46 | 0.39 | 0.55 |  |
| 55 Util(ew) | 0.39 | 0.26 | 0.48 | 0.30 | 0.43 | 0.31 | 0.43 | 0.35 | 0.26 |

Panel B: Value weighted industry indices

|  | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 Material(vw) | 0.41 |  |  |  |  |  |  |  |  |
| 20 Industry(vw) | 0.71 | 0.46 |  |  |  |  |  |  |  |
| 25 ConsDisc(vw) | 0.38 | 0.48 | 0.50 |  |  |  |  |  |  |
| 30 ConsStapl(vw) | 0.55 | 0.40 | 0.58 | 0.45 |  |  |  |  |  |
| 35 Health(vw) | 0.42 | 0.32 | 0.43 | 0.32 | 0.42 |  |  |  |  |
| 40 Finan(vw) | 0.56 | 0.50 | 0.61 | 0.56 | 0.61 | 0.36 |  |  |  |
| 45 IT(vw) | 0.40 | 0.27 | 0.43 | 0.36 | 0.44 | 0.33 | 0.39 |  |  |
| 50 Telecom(vw) | 0.36 | 0.20 | 0.47 | 0.36 | 0.35 | 0.41 | 0.41 | 0.52 |  |
| 55 Util(vw) | 0.34 | 0.27 | 0.43 | 0.29 | 0.44 | 0.39 | 0.43 | 0.37 | 0.33 |

The table shows correlations between monthly returns for 10 industry portfolios grouped by GICS.

## Chapter 9

## A few large stocks

The OSE has always had a few large companies which in terms of market capitalization have a dominant position on the exchange. For many years it was Norsk Hydro, but with the listing of the large, state dominated companies Telenor and Statoil this changed. To illustrate to what degree the exchange is likely to be affected by these large companies table 9.1 shows, for each year, the four largest companies, and each company's fraction of the value of the exchange.

Table 9.1 The four largest companies each year


The table lists the four largest companies on the exchange in terms of the market capitalization. For each company we list the name and the fraction of the market capitalization this company had at yearend.

Figure 9.1 The three largest companies at the OSE


The figure plots the time series evolution of what fraction of the exchange the three largest compenies at the OSE have.

Figure 9.2 The largest companies at the OSE


The figure plots the time series evolution of what fraction of the exchange the largest compenies at the OSE have.

## Chapter 10

## How many stocks are necessary for a well diversified portfolio?

In a first course in finance the concept of risk is usually introduced using a picture like figure 10.1, which illustrates the relationship between the number of stocks in an equally weighted portfolio and the standard deviation of the portfolio. This picture is then used to introduce the difference between systematic and unsystematic risk, where the unsystematic risk is the risk that can be diversified away by increasing the number of stocks in the portfolio. We will not go this route, we will instead look directly at the relationship between number of stocks and standard deviation. This difference can namely be used to say something about when we have achieved "most" of the relevant diversification.

Figure 10.1 Relationship between number of stocks in an equally weighted portfolio and the portfolios standard deviation


Empirical curves like this can be found in any number of classical empirical papers. By creating random portfolios by the well known "Throwing Darts at The Wall Street Journal" method, and increasing the number of stocks in the portfolio, one find empirical versions of the curve in figure 10.1. The curve always has the same shape, the portfolio standard deviation decreases with the number of stocks, but flattens out after a while. The number of stocks at which the curve flattens out is used as a measure of how many stocks are "enough" to achieve most of the diversification. In US papers there is some variation in this number, for example Evans and Archer (1968) argues for 10 stocks being enough, Wagner and Lau (1971) concludes that most of the diversification is achieved at 15 stocks, while Statman (1987) argues for 30 stocks.

We here perform similar calculations as the US papers using data for the Oslo Stock Exchange.

### 10.1 Methods

All stock at the OSE in the period 1980-2016 with a minimum of liquidity is included. ${ }^{1}$ A portfolio is simulated by randomly drawing $n$ shares at the first date. Going forward, each month the return of an equally weighted portfolio of the chosen stocks is calculated. If a stock is delisted, the last observed price is used as the price for realizing the stock, and the stock is replaced by randomly drawing another stock. Stock returns of the simulated trading strategies are calculated for the period 1980 to 2016, and the standard deviation of the portfolio is calculated. This random portfolio construction is repeated 100 times. Finally we calculate the average of these estimated standard deviations.

### 10.2 Results

Figure 10.2 shows results for the whole period. The shape of the curve is similar to what is found in other stock markets. The gains to diversification are obvious, and particularly strong up to five stocks. There is a marked fall down to $10-15$ stocks, but after that the curve levels out, even though it is still decreases down to the maximal portfolio of 40 stocks.

Figure 10.2 Relation between number of stocks and standard deviation for portfolios at OSE


Average standard deviation of monthly portfolio returns for 100 simulated stock portfolio at OSE. Each portfolio is an equally weighted portfolio of $n$ stocks, where $n$ varies along the horizontal axis. Numbers in percent.

In figure 10.3 we split the simulations into two subperiods, 1980-1994and 1995-2016.

### 10.3 How close do we get to a stock market index?

Table 10.1 show detailed results for the various simulations. In addition it shows comparable numbers for two stock market indices, one equally weighted (EW) and one value weighted (VW).

[^4]Figure 10.3 Relation between number of stocks and standard deviation for portfolios at OSE for subperiods Subperiod 1980-1995


Subperiod 1996-2016


Average standard deviation of monthly portfolio returns for 100 simulated stock portfolio at OSE. Each portfolio is an equally weighted portfolio of $n$ stocks, where $n$ varies along the horizontal axis. Numbers in percent. Two subperiods: 1980-1995, 1996-2016

Table 10.1 Relation between number of stocks and standard deviation for portfolios at OSE

| No stocks | Standard Deviation (\%) |  |  |
| :--- | :---: | :---: | :---: |
| in portfolio | $1980-2016$ | $1980-1999$ | $2000-2016$ |
| 1 | 12.79 | 13.25 | 11.52 |
| 2 | 9.63 | 10.28 | 9.47 |
| 3 | 8.80 | 9.32 | 8.17 |
| 4 | 8.22 | 8.79 | 7.71 |
| 5 | 7.76 | 8.52 | 7.00 |
| 6 | 7.48 | 8.04 | 6.65 |
| 7 | 7.23 | 7.83 | 6.57 |
| 8 | 6.96 | 7.62 | 6.39 |
| 9 | 6.99 | 7.45 | 6.28 |
| 10 | 6.74 | 7.35 | 5.88 |
| 11 | 6.66 | 7.27 | 5.96 |
| 12 | 6.53 | 7.20 | 5.90 |
| 13 | 6.53 | 7.07 | 5.59 |
| 14 | 6.45 | 7.05 | 5.65 |
| 15 | 6.44 | 6.95 | 5.62 |
| 16 | 6.37 | 6.90 | 5.48 |
| 17 | 6.27 | 6.89 | 5.56 |
| 18 | 6.24 | 6.91 | 5.53 |
| 19 | 6.26 | 6.82 | 5.41 |
| 20 | 6.18 | 6.87 | 5.41 |
| 21 | 6.15 | 6.76 | 5.38 |
| 22 | 6.12 | 6.75 | 5.39 |
| 23 | 6.12 | 6.74 | 5.36 |
| 24 | 6.09 | 6.71 | 5.36 |
| 25 | 6.12 | 6.65 | 5.32 |
|  | 5.43 | 6.06 |  |
| EW | 6.13 | 6.59 | 4.55 |
| VW |  |  | 5.53 |

Average standard deviation of monthly portfolio returns for 100 simulated stock portfolio at OSE. Each portfolio is an equally weighted portfolio of $n$ stocks, where $n$ varies along the horizontal axis. Numbers in percent. Three subperiods: 1980-1999, 2000-2016 and 1980-2016. At the bottom of the table results for two indices. $E W$ : equally weighted index. $V W$ : value weighted index.

### 10.4 Conclusion

We have seen how many stock are necessary to get a reasonably "well diversified" stock portfolio at the Oslo Stock Exchange. The numbers are essentially comparable to US results, with most of the relevant diversification achieved after 10 stocks. Even though Oslo Stock Exchange is very much smaller than the NYSE, and concentrated in only a few sectors, that the magic number 10 should appear to be valid here too is surprising. The Law of Large Numbers appears to work also at the Oslo Stock Exchange.

## Chapter 11

## The variability of the Oslo Stock Exchange

In this chapter we discuss the variability of stock returns at the OSE. There are different ways of measuring variability. The most common is to look at the volatility, or standard deviation, of returns. We will look at some time series of volatility. Let us first consider the market as a whole, and look at the volatility of market indices. The next way to investigate volatility is to consider individual stocks, and calculate the volatility across stocks.

### 11.0.1 The volatility of market indices

Let us look at the time series evolution of the two indices VW and EW which we have calculated earlier. In figure 11.1 we each year calculate the volatility of that years returns on the market index. In figure 11.2 we do similar calculations at higher frequencies.

Figure 11.1 The annual volatility of market indices at the OSE
EW index


VW index


For each of the indices EW and VW we calculate the volatility of one year of daily returns, and plot the time series of resulting estimates.

Figure 11.2 Higher frequency estimates of volatility of market indices at the OSE
Quarterly estimates


Monthly estimates


For the index EW we calculate the volatility of one quarter(top figure) and one month(bottom figure) of daily returns, and plot the time series of resulting estimates

### 11.0.2 The average volatility across stocks

Instead of looking at the market, it may be more informative to look at the volatility of individual stocks, and ask: What is the average volatility for individual stocks. In figure 11.3 we show such averages, where we calculate the volatility for each stock on the OSE, and then report various averages.

Figure 11.3 Average volatility for all firms at the OSE
Annual calculations


Quarterly calculations


Monthly calculations


The tables show averages of estimated volatility across stocks. For each stock the standard deviation of stock returns is calculated using one year's worth of daily returns (top figure), one quarters worth (middle figure) or one month's worth (bottom figure). These estimates are then averaged across stocks. The calculation is done at the ends of respecitely years, quarters and months. When taking the average we Windsorize the data by removing the most extreme one percent. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

Figure 11.4 Average volatility for size sorted portfolios, firms at the OSE
Annual data


Quarterly data


Monthly data


The tables show averages of estimated volatility across stocks. For each stock the standard deviation of stock returns is calculated using one year's worth of daily returns (top figure), one quarters worth ( $4 \boldsymbol{T}$ ddle figure) or one month's worth (bottom figure). We then group stocks into four portfolios based on firm size, and average across these portfolios. Data for stocks listed at the Oslo Stock Exchange during the period 1980-2016.

## Chapter 12

## Time series properties at the Oslo Stock Exchange

### 12.0.1 Observations on market indices

Let us look at the time series evolution of the two indices VW and EW which we have calculated earlier. In figure 12.1 we each year calculate the (first order) autocorrelation of that years returns.

Figure 12.1 The annual autocorrelations of market indices at the OSE
EW index


For each of the indices EW and VW we calculate the autocorrelation (lag one) of one year of daily returns, and plot the time series of resulting estimates.

Table 12.1 shows estimates of autocorrelations for various market indices, for the whole period 1980 to 2016, and for subperiods.

| Index ew(daily) |  | 1980-2016 | 1980-1989 | 1990-1999 | 2000-2016 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | 0.0011 | 0.0013 | 0.0012 | 0.0009 |
|  | Stdev | 0.009 | 0.009 | 0.010 | 0.009 |
|  | Autocorr(1) | 0.12 | 0.19 | 0.12 | 0.06 |
|  | Autocorr(2) | 0.04 | 0.07 | 0.04 | 0.03 |
| ew(weekly) | Mean | 0.0045 | 0.0062 | 0.0046 | 0.0034 |
|  | Stdev | 0.024 | 0.027 | 0.025 | 0.021 |
|  | Autocorr(1) | 0.11 | 0.15 | 0.17 | 0.01 |
|  | Autocorr(2) | 0.09 | 0.08 | 0.15 | 0.04 |
| ew(monthly) | Mean | 0.0167 | 0.0235 | 0.0160 | 0.0132 |
|  | Stdev | 0.054 | 0.061 | 0.060 | 0.046 |
|  | Autocorr(1) | 0.28 | 0.22 | 0.30 | 0.30 |
|  | Autocorr(2) | 0.09 | -0.05 | 0.17 | 0.11 |
| vw(daily) | Mean | 0.0010 | 0.0012 | 0.0010 | 0.0009 |
|  | Stdev | 0.013 | 0.012 | 0.012 | 0.014 |
|  | Autocorr(1) | 0.06 | 0.15 | 0.11 | -0.00 |
|  | Autocorr(2) | -0.02 | -0.02 | -0.02 | -0.02 |
| vw(weekly) | Mean | 0.0045 | 0.0054 | 0.0046 | 0.0040 |
|  | Stdev | 0.030 | 0.029 | 0.029 | 0.030 |
|  | Autocorr(1) | -0.01 | 0.10 | 0.05 | -0.09 |
|  | Autocorr(2) | 0.04 | 0.14 | 0.09 | -0.04 |
| vw(monthly) | Mean | 0.0186 | 0.0236 | 0.0184 | 0.0158 |
|  | Stdev | 0.061 | 0.070 | 0.061 | 0.055 |
|  | Autocorr(1) | 0.15 | 0.16 | 0.10 | 0.17 |
|  | Autocorr(2) | -0.04 | -0.18 | -0.02 | 0.04 |

### 12.0.2 Autocorrelation of individual stocks

Table 12.2 Autocorrelation of individual stock returns
Panel A: Averages across all stocks


Panel B: Quartile plots


## Chapter 13

## Calendar effects

There is a large empirical literature in finance on the general topic of calendar effects, which can be summarized as predictable variation in stock returns based on calendar time. At first glance such effects may sound like a violation of market efficiency, if we have in mind the classical "random walk" theory of efficiet markets. However, such effects may be consistent with a version of market efficiency where risk premia changes over time, or with some market imperfections inducing such predictability. In particular, there are some predictability in returns based on the month

In this chapter we replicate some of the standard investigations using data from the OSE.

### 13.1 Variations in daily returns over the week

We calculate daily stock returns and group the returns by the day of the week.
Table 13.1 Day of the week effects

| Weekday | EW | VW | TOTINDX | OBX |
| :--- | :---: | :---: | :---: | :---: |
| Monday | 0.05 | 0.04 | 0.00 | -0.04 |
| Tuesday | 0.06 | 0.05 | 0.03 | 0.03 |
| Wednesday | 0.10 | 0.09 | 0.03 | 0.03 |
| Thursday | 0.13 | 0.15 | 0.09 | 0.08 |
| Friday | 0.22 | 0.17 | 0.14 | 0.12 |

The table shows percentage daily returns split on day of the week.

Table 13.2 Friday the thirteenth

|  | EW |  | VW |  | TOT |  | OBX |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Fridays | 0.22 |  | 0.17 |  | 0.14 | 0.12 |  |  |
| Friday thirteenths | 0.28 | 62 | 0.24 | 62 | 0.27 | 56 | 0.26 |  |
| Other Fridays | 0.22 | 1793 | 0.17 | 1793 | 0.14 | 1623 | 0.12 |  | 1430

The table shows percentage daily returns.

### 13.2 Variation in daily returns over the month

Ariel (1987) looks at this in the US.
Table 13.3 Day of the month effects

| Day | EW | VW | TOTINDX | OBX |
| :--- | :---: | :---: | :---: | :---: |
| 1 | 0.05 | 0.12 | 0.18 | 0.23 |
| 2 | 0.20 | 0.29 | 0.25 | 0.28 |
| 3 | 0.15 | 0.10 | 0.08 | 0.09 |
| 4 | 0.13 | 0.12 | 0.08 | 0.07 |
| 5 | 0.09 | 0.05 | -0.01 | -0.07 |
| 6 | 0.20 | 0.20 | 0.11 | 0.09 |
| 7 | 0.09 | 0.11 | 0.04 | -0.01 |
| 8 | 0.09 | 0.04 | -0.03 | -0.04 |
| 9 | 0.14 | 0.07 | 0.07 | 0.09 |
| 10 | 0.08 | 0.06 | -0.01 | -0.06 |
| 11 | 0.11 | 0.11 | 0.05 | 0.01 |
| 12 | 0.08 | -0.00 | -0.06 | -0.15 |
| 13 | 0.12 | 0.13 | 0.10 | 0.13 |
| 14 | 0.15 | 0.15 | 0.06 | 0.12 |
| 15 | 0.06 | 0.01 | -0.03 | -0.05 |
| 16 | 0.07 | 0.12 | 0.05 | 0.06 |
| 17 | 0.21 | 0.15 | 0.14 | 0.13 |
| 18 | 0.04 | 0.09 | 0.02 | 0.05 |
| 19 | 0.02 | 0.05 | -0.02 | -0.03 |
| 20 | -0.03 | -0.04 | -0.12 | -0.14 |
| 21 | 0.11 | 0.16 | 0.13 | 0.13 |
| 22 | 0.07 | 0.06 | 0.03 | -0.02 |
| 23 | 0.13 | 0.12 | 0.05 | 0.08 |
| 24 | -0.00 | -0.06 | -0.11 | -0.12 |
| 25 | 0.07 | 0.03 | 0.01 | -0.02 |
| 26 | 0.10 | 0.08 | 0.04 | 0.04 |
| 27 | 0.18 | 0.20 | 0.17 | 0.14 |
| 28 | 0.09 | 0.00 | 0.01 | -0.00 |
| 29 | 0.17 | 0.17 | 0.17 | 0.16 |
| 30 | 0.36 | 0.27 | 0.25 | 0.18 |
| 31 | 0.23 | 0.18 | 0.15 | 0.14 |

The table shows percentage daily returns split on day of the month.

### 13.3 Variation in monthly returns over the year

The best known empirical regularity in the US is the January effect.
Table 13.4 Monthly effects

| Month | EW | VW | TOT | OBX |
| :--- | ---: | ---: | ---: | ---: |
| Jan | 5.4 | 3.7 | 3.1 | 1.7 |
| Feb | 2.9 | 2.1 | 1.8 | 2.1 |
| Mar | 2.3 | 1.9 | 2.2 | 2.3 |
| Apr | 3.2 | 4.3 | 3.6 | 2.8 |
| May | 1.5 | 2.2 | 1.4 | 1.0 |
| Jun | -0.6 | -0.2 | -0.8 | -0.5 |
| Jul | 2.7 | 3.1 | 2.6 | 2.7 |
| Aug | 0.1 | 0.6 | -0.5 | -1.1 |
| Sep | -0.9 | -0.6 | -1.5 | -2.2 |
| Oct | 0.9 | 1.7 | 0.5 | 0.3 |
| Nov | 0.4 | 0.3 | -0.4 | -0.5 |
| Dec | 2.2 | 3.2 | 2.8 | 2.9 |

The table shows percentage monthly returns split by month.

Table 13.5 Monthly effects, by size portfolios
Whole period, 1980-2016

| Month | 1(small) | 2 | 3 | 4 | 5 (large) |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Jan | 8.6 | 5.5 | 5.7 | 4.1 | 2.8 |
| Feb | 4.7 | 2.9 | 3.6 | 2.3 | 1.2 |
| Mar | 3.1 | 2.5 | 2.1 | 2.1 | 1.7 |
| Apr | 3.5 | 3.2 | 3.4 | 2.9 | 3.0 |
| May | 1.9 | 1.5 | 1.5 | 1.9 | 1.0 |
| Jun | 0.3 | -0.3 | -0.6 | -1.0 | -1.4 |
| Jul | 3.4 | 2.2 | 2.3 | 2.5 | 3.3 |
| Aug | 1.1 | 0.1 | 0.0 | -0.3 | -0.8 |
| Sep | 0.7 | -0.6 | -1.1 | -2.0 | -1.7 |
| Oct | 0.4 | 1.2 | 1.2 | 0.9 | 0.7 |
| Nov | 1.7 | -0.1 | 0.2 | 0.6 | -0.1 |
| Dec | 1.0 | 0.8 | 2.9 | 3.5 | 2.7 |

Table 13.6 Monthly effects, by size portfolios, split in subperiods
Panel A: Subperiod 1980-1989

| Month | 1(small) | 2 | 3 | 4 | 5 (large) |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Jan | 15.4 | 9.8 | 9.9 | 6.8 | 7.0 |
| Feb | 6.3 | 1.9 | 4.2 | 1.6 | 0.7 |
| Mar | 6.4 | 4.2 | 2.6 | 1.9 | 1.7 |
| Apr | 4.2 | 5.1 | 4.0 | 3.3 | 4.2 |
| May | 0.3 | -1.3 | 0.3 | 0.1 | -0.7 |
| Jun | -0.8 | -1.8 | -1.5 | -2.5 | -1.2 |
| Jul | 5.6 | 4.2 | 3.3 | 3.7 | 5.0 |
| Aug | 2.5 | 1.4 | 0.2 | 2.4 | 2.0 |
| Sep | 4.1 | 0.2 | 1.5 | 1.6 | 1.1 |
| Oct | -0.6 | 0.1 | 2.1 | -0.6 | -2.5 |
| Nov | 3.9 | -0.5 | 0.0 | -0.2 | -1.0 |
| Dec | 0.2 | 0.6 | 2.2 | 4.6 | 1.7 |

Panel B: Whole period, 1990-1999

| Month | 1(small) | 2 | 3 | 4 | 5 (large) |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Jan | 8.0 | 6.3 | 6.1 | 4.6 | 3.9 |
| Feb | 5.8 | 5.5 | 3.6 | 1.2 | 1.0 |
| Mar | 3.6 | 3.1 | 2.8 | 3.2 | 2.6 |
| Apr | 5.7 | 2.6 | 4.3 | 2.7 | 2.6 |
| May | 4.6 | 3.3 | 2.4 | 3.7 | 2.1 |
| Jun | 0.5 | -0.5 | -0.9 | -1.5 | -1.6 |
| Jul | 3.7 | 1.7 | 2.4 | 2.6 | 3.5 |
| Aug | -0.3 | -1.5 | -1.8 | -4.3 | -4.6 |
| Sep | -0.7 | -1.3 | -2.6 | -5.1 | -2.9 |
| Oct | -0.0 | 1.2 | 0.9 | 1.3 | 2.6 |
| Nov | -0.5 | -1.1 | -0.9 | -0.9 | -1.2 |
| Dec | 2.2 | 0.7 | 2.6 | 2.5 | 4.2 |

Panel C: Subperiod 2000-2016

| Month | 1(small) | 2 | 3 | 4 | 5 (large) |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Jan | 5.0 | 2.4 | 3.0 | 2.2 | -0.3 |
| Feb | 3.2 | 2.0 | 3.2 | 3.2 | 1.6 |
| Mar | 0.9 | 1.2 | 1.3 | 1.6 | 1.1 |
| Apr | 1.8 | 2.5 | 2.6 | 2.9 | 2.6 |
| May | 1.2 | 2.0 | 1.7 | 1.9 | 1.3 |
| Jun | 0.7 | 0.7 | 0.2 | 0.2 | -1.3 |
| Jul | 2.0 | 1.3 | 1.6 | 1.8 | 2.2 |
| Aug | 1.2 | 0.3 | 1.1 | 0.5 | -0.3 |
| Sep | -0.5 | -0.7 | -1.9 | -2.4 | -2.7 |
| Oct | 1.2 | 1.8 | 1.0 | 1.5 | 1.5 |
| Nov | 1.6 | 0.8 | 1.0 | 2.0 | 1.0 |
| Dec | 0.8 | 0.9 | 3.4 | 3.5 | 2.5 |

The table shows percentage monthly returns split by month. Size portfolios.

## Chapter 14

## Interest Rates

In this chapter we discuss interest rate data.
For this paper we limit ourselves to estimates of two different interest rate series, a short term (monthly) risk free rate and an annual risk free rate. For details about Norwegian interest rate data we refer to (Eitrheim et al., 2006, Ch 6). For most of the period we use interbank rates, NIBOR as the estimate of the risk free rate. Both monthly and annual NIBOR rates are available from 1986. The period before 1986 is slightly "messy" regarding interest rate data, and we need to use some imperfect proxies. For monthly risk free interest from 1982 to 1986 we use the overnight NIBOR rate as an approximation. Before 1982 for the monthly data, and before 1986 for the annual data, we use the shortest possible bond yield for treasuries in Eitrheim et al. (2006) as estimates for interest rates. For the 1980 to 86 period this means we use the two year bond yield as an estimate of the risk free rate.

Figure 14 plots the monthly risk free interest rate. The "spike" in the interest rate in 1992 is due to a currency crisis.

Figure 14.1 Short term (monthly) risk free interest rate


The figure plots annualized percentage one month interest rate for the period 1980 to 2016.

For some of the longer term calculations we also use the annual (one year) interest rate. Figure 14 illustrates this interest rate.

Figure 14.2 One year risk free interest rate


The figure plots annualized percentage one year interest rate for the period 1980 to 2016.

### 14.1 Sources

All interest rate data is available from the webcite of the Central Bank of Norway (www.norges-bank.no).

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[^0]:    ${ }^{1}$ It should be noted that filtering such as this is very common for asset pricing investigations of this sort. See for example Fama and French (1992).

[^1]:    ${ }^{1}$ The indices do however not account for repurchases.

[^2]:    ${ }^{2}$ See the literature starting with Mehra and Prescott (1985). A survey is provided in Kocherlakota (1996).

[^3]:    ${ }^{3}$ See chapter 14 for some data on interest rates.

[^4]:    ${ }^{1}$ The filter criteria discussed in chapter 6 are applied, stocks traded less than 20 days a year, and stocks with prices below 10 are removed.

